



IMAGE ENCRYPTION BASED ON WALSH HADAMARD TRANSFORM

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Abstract

In this paper, we introduce encryption algorithm have computational complexity, image cryptography application based on Walsh-Hadamard transform. The proposed method consists of image transformation at different level and scrambles the components to design image encryption algorithm. The proposed encryption techniques having unique parameter (key) like order of transform, position of row and column. These unique parameters help to design image encryption algorithm. Original image can be reconstructed when user is known to key parameter. We analyze proposed technique and also represent encryption time for each decomposition level. The results prove that proposed method having high security as compared to state of art methods.

Keywords: Data security, Image encryption, Walsh-Hadamard Transform.

1. Introduction

Signal processing in encrypted domain (SPED) has received attention in recent year. The main motto is to protect user data from unauthorized user. In most of the technologies, data like image, video, text are transfer on large extent across the multimedia and network system [1-5]. In military, medical and various field, it is required to transmit the data which should be secure. To provide such facility, image cryptography plays vital role. Therefore, it is mandatory to design image encryption algorithm to ensure security across various network system. Many researchers designed various encryption techniques. Discrete Fourier Transform (DFT) and Discrete Cosine Transform (DCT) based algorithm implemented in [6]. Discrete Wavelet Transform in encrypted domain (DWT) is studied and data scrambling method is introduced in [7]. Face verification using quasi homomorphic encryption is executed with intervals [8-9]. New approach is introduced using block cipher by performing nonlinear operations. Chaos technique implemented by selecting confusion and diffusion in many rounds. Lossless and reversible data hiding process is introduces in encryption domain [10-15]. Walsh Hadamard Technique (WHT) is widely used in signal processing for various application such as image compression [16], coding [17], communication and filtering [18]. Main feature of WHT is that calculation doesn't involve division and multiplication, WHT is used in video compression i.e. H.264/MPEG-4 AVC format and VP9 [19]. The quality of

encryption algorithm is decided by complexity of mathematical calculation. WHT method is widely used in signal processing for various application like bioinformatics, multimedia data, filtering, and array analysis. Many times, attacker can retrieve data by manipulating system algorithm [20-22]. To address this problem, we have scrambled the order of key parameters. By decomposing input image and shuffling the parameters, we can secure the image. This paper represents the new encryption method using WHT [23]. Key parameters are arranged as stack format in Bookkeeping vector which consist of number of decomposition components, decomposition technique and the order of key parameters. The encryption algorithm can be designed by selecting appropriate parameters. This paper is organized as follows: Review of Walsh Hadamard Transform briefly explained in section II. Image encryption technique is proposed in section III. Section IV brief about experiment using WHT and result discussion and conclusion in section V.

2. PREVIEW OF WALSH HADAMARD TRANSFORM

The WHT consist of natural ordering, dyadic ordering and sequence ordering, let we define parameter like

$$H_1 = [1] \text{ and } H_2 = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} H_1 & H_1 \\ H_1 & -H_1 \end{bmatrix}$$

Recursive matrix of WHT is starting from H2. In proposed method, we exclude the scale vector in H2 for simplification to apply WHT in encrypted domain [24].

1) Hadamard Ordering: $H_{h,M}$ of size $M \times M$ Hadamard transform obtained using recursive relation:

$$H_{h,M} = H_2 \otimes H_{h,M/2} = \begin{bmatrix} H_{h,2^{g-1}} & H_{h,2^{g-1}} \\ H_{h,2^{g-1}} & -H_{h,2^{g-1}} \end{bmatrix} \quad (1)$$

Where, $g = \log_2 M$, $g = 1, 2, 3 \dots$ and \otimes is Kronecker product operator

2) Paley Ordering: Paley ordered transform matrices can be given as:

$$H_{p,M} = (H_2 \otimes H_{p,M/2}) P_{2,M/2}^T \quad (2)$$

Where, $P_{2,M/2}$ is a perfect shuffle matrix and $(\cdot)^T$ is the matrix transposition operator.

3) Walsh Ordering: The Walsh ordered WHT is widely used in signal processing theory. Walsh ordering transform is given by:

$$H_{w,M} = (H_2 \otimes H_{w,M/2}) P_{2,M/2}^T \left(E_{M/4} \otimes \begin{bmatrix} 1000 \\ 0100 \\ 0001 \\ 0010 \end{bmatrix} \right) \quad (3)$$

Where, E_M is identity matrix of size $M \times M$

Definition of two dimensional WHT is given by:

$$\hat{V}(m, n) = \frac{1}{M} \sum_{i=0}^{M-1} \sum_{j=0}^{M-1} H_g(m, i) X(i, j) H_g(j, n), m, n = 0, 1, \dots, M-1 \quad (4)$$

Where, X is input image of size $M \times M$.

3. Design Methodology: Image Encryption Based on Walsh Hadamard Transform

In this section, we propose image encryption using WHT technique. We decompose input image using Walsh Hadamard technique.

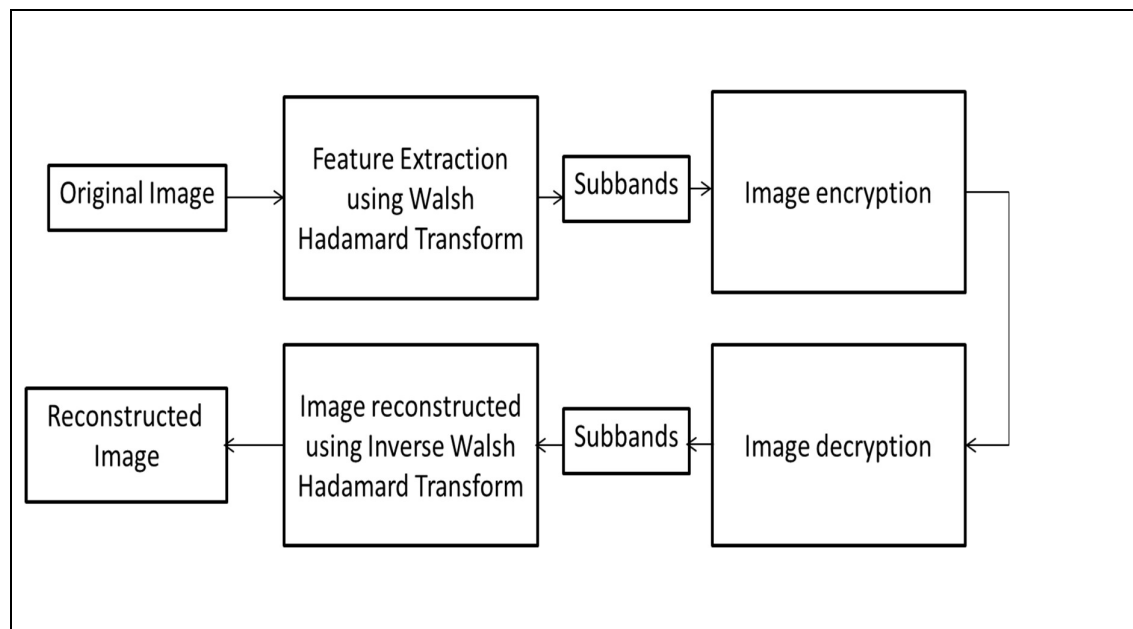


Fig.1. Image Encryption

Walsh Hadamard Transform is adapted for various application such as image compression, image transform coding, image watermarking. The proposed method is explained in Fig. 1. In this method, features of input image size $M * N$ are extracted using WHT. Proposed transform is applied to input image at particular order and row/column of transformed image is scrambled in random manner. The key parameters after transformation i.e. order WHT and positioning of rows and columns is used for image encryption. Original image is reconstructed using inverse WHT. In proposed method, order of Walsh Hadamard transform and positioning of row/column of transformed image act as key parameters. Key parameters like order of Walsh Hadamard transform and positioning of row/column of transformed image are arranged in stack format which is very unique and known to user only. Anybody can decrypt the original image only when user known key parameters.

4. Experimentation and Result

For experimentation purpose, we have applied encryption method on standard images with

size of 256×256 like Cameraman, Peppers, Lena, Barbara, Baboon images as shown in Fig. 2(i)-(v). We used MATLAB with system memory 4GB and Intel core 3 processor. Walsh Hadamard Transform coefficient and reconstructed image is shown in in Fig. 2(vi)-(x) and 2(xi)-(xv). Correlation between original and reconstructed image determine the quality of encryption method [25]. Correlation coefficient for various images is given in Table 1.

Table1. Proposed correlation coefficient of image

Image	Correlation
Cameraman	0.0690
Peppers	0.0773
Lena	0.0594
Barbara	0.0640
Baboon	0.0522

The encryption time for each decomposition level is tabulated in Table 2.

Table.2. Encryption time for decomposition level

Decomposition level	Speed of encryption in second
I	0.0235
II	0.01345
III	0.01744
IV	0.01824
V	0.01984

The effectiveness algorithm is proved by comparing with the proposed algorithm with the state of art techniques. Correlation coefficient of Lena image using proposed design is compared with existing methods like parameterized halfband filterbank (PHFB) approach [08], discrete wavelet transform (DWT) [23], Fresnel transform [26] shown in Table 3. It is observed that proposed algorithm has less correlation as compared latest methods which ensure more security.

Table.3 Comparison with latest algorithms

Method	Correlation Coefficient
PHFBs [08]	0.07235
DWT [23]	0.09813
Fresnel Transform [26]	0.0821
Proposed Method	0.0594

5. CONCLUSION

This paper introduces new technique of image encryption based on Walsh Hadamard

transform. Order of Walsh Hadamard transforms and positioning of row/column of transformed image act as key parameters. Proposed algorithm has less correlation coefficient between input and encrypted image as compared with latest method. It has been ensured that proposed algorithm offer high security which difficult to crack.

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